The Fizeau Experiment:
Experimental Investigations of the Relativistic Doppler Effect

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We built a Fizeau interferometer that takes advantage of laser light, digital image capture and computer analysis to reproduce the celebrated experiments of Fizeau, Michelson & Morley, and Zeeman, concerning the optics of bodies in relative motion. Like Fizeau, Michelson & Morley, and Zeeman, we found that the zeroth-order central fringe shifts in a velocity-difference-dependent manner. The experimentally-observed fringe displacement was 0.0419 per m/s. If the fringe shift resulted from the linear addition of the velocity of light in water and the velocity of the water, as predicted by Newtonian kinematic theory, the fringe shift would be 0.0784 per m/s. If the fringe shift resulted from the nonlinear addition of the velocity of light in water and the velocity of water, as predicted by the kinematics of the Special Theory of Relativity, the fringe shift would be 0.0151 per m/s. If the fringe shift resulted from the relativistic Doppler-induced transformation of the wavelength of light flowing with and against the water, the fringe shift would be 0.0441 per m/s. We found that the magnitude of the experimentally-observed fringe shift is most accurately accounted for by considering the moving water to cause a relativistic Doppler-induced change in the wavelength of light.

1. Introduction

Einstein [1] considered Fizeau’s aether drag experiment to be an experimentum crucis in deciding between the Newtonian velocity addition law, which is based on absolute time, and the velocity addition law consistent with Special Theory of Relativity, which is based on the relativity of time. The Fizeau experiment [2-4] measured the effect of moving water on the interference pattern produced by two beams of light—one moving parallel to the water velocity and the other moving antiparallel to the water velocity. Fizeau found that the observed displacement of the interference pattern was smaller than that predicted to occur if the velocity of the water through which the light propagated was simply added to the velocity of light traveling parallel to the water and simply subtracted from the velocity of light traveling antiparallel to the water. The conclusion that the velocities were not simply additive were confirmed by the celebrated experimentalists, Michelson & Morley [5] and Zeeman [6,7].

Von Laue [8] interpreted the lack of simple additivity of the velocities consistent with Newtonian kinematic theory to be a direct consequence of the relativity of time posited by the Special Theory of Relativity. Einstein [1] wrote that the Fizeau experiment “decides in favour of [the velocity addition law] derived from the theory of relativity, and the agreement is, indeed, very exact. According to recent and most excellent measurements by Zeeman, the influence of the velocity of flow v on the propagation of light is represented by [the velocity addition law] to within one percent”. Recently, Lahaye et al. [9] described the Fizeau experiment as “a crucial turning point between old and modern conceptions of light and space-time” and they “believe this makes its replication particularly valuable from a pedagogical point of view.”

In a paper published in this journal, Mears and Wayne [10] showed that the magnitude of the fringe shifts observed by Fizeau, Michelson & Morley, and Zeeman could be accounted for in terms of absolute time by considering the beam of light traveling parallel to the water was to be red-shifted by the Doppler effect and the beam of light traveling antiparallel to the water was to be blue-shifted by the Doppler effect. This explanation accounts for the combined results obtained by
Fizeau, Michelson & Morley, and Zeeman with greater than twice the accuracy than the explanation given by the Special Theory of Relativity [10]. Curiously, even though the Doppler Effect is readily perceived when there is relative motion, standard theories rarely, if ever, include the Doppler effect as a primary consideration in the study and description of relative motion. Our work is unique in that it incorporates the relativistic Doppler Effect from the beginning. When expanded to second order, the inclusion of the Doppler effect makes it possible to unify many aspects of mechanics, electrodynamics and optics that are usually treated separately. Indeed, the Doppler effect expanded to second order combined with absolute time also provides alternative derivations of results familiar from the Special Theory of Relativity describing the relativity of simultaneity [11], the arrow of time [12], and why charged particles cannot exceed the vacuum speed of light [13].

The Special Theory of Relativity explains the results of the Fizeau experiment using kinematics as opposed to the theory proffered by Mears and Wayne that explains the results of the Fizeau experiment as a velocity-induced transformation of waveforms [14] that result from the relativistic Doppler effect. Here we have reconstructed the Fizeau experiment using a laser, a video camera, image processing software and computer-assisted analysis. Our results confirm that the theory proffered by Mears and Wayne [10] accounts for the experimental results of the Fizeau experiment more accurately than does the Special Theory of Relativity.

2. Materials and Methods

Construction of the interferometer. This interferometer, like that built by Lahaye et al. [9], is simple and inexpensive enough to be used in high school and undergraduate physics laboratories or in science fairs. We constructed an interferometer based on Michelson & Morley’s design [5] except that the prism used in their interferometer was replaced with mirrors (Figs. 1 and 2). A 532 nm green laser pointer (Model 10098; xUMP.com) provided the light source. The laser was leveled by measuring the height of the laser beam as we projected it across the laboratory. The laser light was shaped by an adjustable slit (Model 125096; Proindustrial.com) and was directed onto a beam splitter composed of a two inch by two inch half-silvered glass plate with 50% transmission and 50% reflection (Part # 45-854; Edmund Optics). The beam splitter was mounted on a two inch by two inch kinematic mount (Part # 58-861, Edmund Optics, Barrington, NJ USA). The four optically flat 20 front surface mirrors 12.7 mm in diameter (Part # 43-400533; Edmund Optics, Barrington, NY USA) were each mounted on a 0.5 inch diameter three screw kinematic mount (Part # 58-853; Edmund Optics). Mirrors 1 and 4 were oriented 67.5 degrees relative to the plane of the half-silvered mirror. Mirrors 2 and 3 were oriented 45 degrees relative to the plane of the half-silvered mirror. The light in the interferometer propagated through copper tubes (½ inch L Mueller copper tube available from local hardware stores). The tubes were five feet long with an internal diameter of 1.27 cm. The two tubes were terminated on all ends with ½ inch to 1¼ inch diameter couplers and 1¼ inch diameter T-junctions to minimize the flow reductions due to the turns. A flat brass ½ inch-hole washer was welded on the terminal end of each T-junction. On one end of the two pipes, the two T-junctions were welded together with a copper tube so that the tubes formed a “U” shape and the two arms of the “U” were approximately 9.5 cm apart. The T-junctions at the ends of the tubes were closed with 3.3 mm thick BOROFLOAT windows (Part # 48-543; Edmund Optics) secured to the brass washers with Loctite 5 min quickset epoxy (Henkel Corp, Rocky Hill, CT USA). We mixed the epoxy and let it sit for approximately four minutes before spreading a thin yet complete layer around the outside of the brass washers. We then strongly pressed on the window and held the window firmly while maintaining pressure for five minutes to allow the epoxy to cure. We had to be careful not to let the epoxy seep too much into the window area or this would disrupt the laser's path. The ends of the copper tubes were approximately 1 cm from the glass windows. This adds some uncertainty on the order of 0.1% in determining the actual optical path length of the flowing water in the interferometer tubes. The tubes of the interferometer were mounted on a two meter long optical rail (Oriel Corp., Stratford, CT USA).
Fig. 1: Schematic of the Fizeau interferometer used in the present experiment. M1, M2, M3 and M4 are mirrors; S is a variable slit; BS is a beam splitter made from a half-silvered mirror and ND is a neutral density filter. I is the water input, O is the water output and FM is the flow meter. The water flows through the interferometer with a clockwise sense as viewed from above. Path one propagates through the interferometer parallel to the water flow with a clockwise sense while path two propagates through the interferometer antiparallel to the water flow with an anticlockwise sense.

Fig. 2: A) Actual Fizeau interferometer with insets of B) flow meter and C) digital camera.
The interference pattern (Fig. 3) was captured with a 9 MP digital camera (AmScope, Irvine, CA) mounted on a microscope body so that its height could be adjusted. Due to space limitations, the sensor was placed at “optical infinity” approximately 1.3 m from the half-silvered mirror. A 2 O.D. neutral density filter (03FNG023; Melles Griot, Rochester, NY USA) was placed in front of the camera; perpendicular to the beams so that the exposure time was increased to around 10-30 ms. When the neutral density filter was not correctly aligned, the intensity of the interference patterns changed when the water flow changed.

Fig.3: Image of the interference pattern captured with the AmScope digital camera and Toup View image processing software.

The water flowed from the tap through a valve that controlled the water flow (Fig. 2). The water then flowed through an 18 inch piece of nipple pipe with ½ inch NPT ends through the calibrated FlowStat sensor, through another 18 inch length of nipple pipe and lastly through approximately 50 cm of vinyl tubing (3/4 inch OD x 5/8 inch ID) into the bottom of the interferometer, adjacent to mirror 3. The segments of vinyl tubing provided some isolation from vibration and visual detection of air bubbles.

The water flowed out of the top of the interferometer, adjacent to mirror 2, through approximately 10 cm of vinyl tubes (1¼ inch OD x 1 inch ID), then through approximately 1½ meters of copper tubing (1 1/8 inch OD x 1 inch ID), and then through approximately 80 cm of vinyl tubing (1¼ inch OD x 1 inch ID) which terminated in a water-filled beaker filled with water that prevented the introduction of air bubbles backing up into the system (Fig. 3).

The temperature of the building-supplied tap water was measured with an Accumet Model 925 pH meter equipped with a temperature probe (Model 13-620-17; Fisher Scientific, Pittsburgh, PA USA). The water temperature varied throughout the year, but was usually relatively stable during an experiment (±0.1 C). When the water was too cold, on a humid day, it could introduce condensation on the windows which degraded the interference pattern. We solved this problem by using a dehumidifier (Amana Model DM70E-E; Haier America, New York, NY). On the other hand, when the water was too warm, dissolved gases would come out of solution and introduce bubbles that also degraded the interference pattern. We initially used building-supplied reverse-phase osmosis deionized water directly from a faucet or from a carboy placed above the interferometer in the plenum space above the suspended ceiling, but we could not get the high flow rates that we could get with the tap water.

The flow rate of water was measured with a calibrated FlowStat 0.75-7.5 GPM sensor (InstruMart, S. Burlington, VT USA) which has an accuracy of 2% of full scale. The output of the sensor was calibrated at the factory so that the slope of the DC output was 5V/7.5 GPM. The output was read from a digital voltmeter (Model 22-806; Radio Shack, Fort Worth, TX). The temporal variation (± 4%) in the water pressure was probably the greatest cause of variability in the results. We minimized the variability by obtaining pairs of interference patterns obtained with a faster flow and a slower flow within about 30-60 s. In general the flow rate was more stable nights and weekends, although good data could be obtained during the weekdays and we often had visitors conduct experiments during the work day, with results consistent with the data presented. The data presented in this paper were obtained between the end of the final exam period and graduation, when the majority of students left campus and we had fewer people with whom to share the water. At this time, the maximum water velocity through the interferometer increased about 12% from about 3.2 m/s to about 3.6 m/s. The velocity difference \( \nu \) was calculated with the following formula:

\[
\nu = 0.77146 \left( V_{\text{fast}} - V_{\text{slow}} \right) \tag{1}
\]

Where, \( V \) is the voltage output from the flow meter, and 0.77146 is an instrument-specific factor derived from the voltage to flow rate ratio of the sensor (\( X = 7.5 \text{ GPM/5 V} \)), the conversion factor
needed to convert GPM to m³/s, and the cross sectional area $A = 1.2267 \times 10^{-4} m^2$ of the copper pipe in the interferometer. The constant that relates the velocity difference to the voltage difference is:

$$\frac{x_C}{A} = 0.77146 \quad (2)$$

The flow can be described by its Reynolds Number $Re$:

$$Re \approx \frac{\nu \rho x}{\eta} \quad (3)$$

Where, $\nu$ varied from 0 to 3.6 m/s, the water density $\rho = 10^3$ kg/m³, the characteristic length or diameter of the pipe $x = 2.54 \times 10^{-2} m$ and the viscosity of the water $\eta = 0.001$ Pa s. The Reynolds Numbers that describe the flow of water through the pipes in the interferometer vary from $Re \approx 12,700$ for flows of 0.5 m/s to $Re \approx 91,440$ for flows of 3.6 m/s. These Reynolds Numbers are all greater than 2,300, indicating that the flow is turbulent [15]. Fizeau [4], Michelson & Morley [5], Zeeman [7] and Lahaye et al. [9] estimate that the ratio of the maximal velocity where the light beams propagate to the average velocity that is measured is approximately equal to 1.16. Consequently, the predicted theoretical fringe shifts for a given measured velocity have been multiplied by 1.16.

The pattern of the water flow is not simple. In principle, it would be possible to construct models that could predict some of the effects of accelerations around the corners of the interferometer, however, despite the significant effort that would be required; the residual uncertainty is still likely to be unacceptable to apply as a correction to the experiment. Consequently, we accept our ignorance concerning localized accelerations and consider the velocities to be constant in the straight sections of tube through which the light beams travelled.

**Method of alignment.** Before aligning the interferometer, we let the tap water run for at least half an hour to allow the system to stabilize. We aligned the interferometer while water was running through it with a velocity of approximately 1.5 m/s. One of the light paths was blocked by placing a card in front of either mirror 1 or mirror 4. This allowed us to isolate one light path at a time. From here we could align both the (1) clockwise and (2) anticlockwise light paths independently. Light propagating along path (1) propagated through the half-silvered mirror to mirror 1, to mirror 2, to mirror 3, to mirror 4 and back through the half-silvered mirror. Light propagating along path (2) reflected off the half-silvered mirror to mirror 4, to mirror 3, to mirror 2, to mirror 1 and reflected off the half-silvered mirror. The laser is centered on mirror 1 and the half-silvered mirror is adjusted to also center the laser on mirror 4. We sequentially adjusted each of the four mirrors so that each light path propagated through the center of the copper pipes in opposite directions. We made sure that the two light paths were superimposed on each window. The sensor of the camera was placed so that the two beams were centered on it and the sensor was perpendicular to the beam. The neutral density filter was slightly inclined so as to reflect the light slightly below mirrors 1 and 4 so that the reflected light would not be superimposed on the light passing through the interferometer tubes. The two superimposed beams (Fig. 4) were centered on the camera sensor and on the digitally-marked center line on computer monitor.

![Fig. 4: The two beams are superimposed on the camera sensor and on the computer monitor.](image)

The interference pattern was generated by translating mirrors 1 and 4 simultaneously so that the two superimposed beams separated horizontally just enough to form a vertical zeroth-order central fringe, corresponding to equal path lengths. The zeroth-order central fringe (Fig. 5) formed on the digitally-marked central line. A variable slit was inserted into the path between the laser and the half-silvered mirror. The slit was narrowed until the fringes were sharp (Fig. 3). When an inclined glass plate was placed in front of window 4, the width and inclination, but not the center position, of the central fringe was affected by the oblique refraction of the beam.
The zeroth-order central fringe could be formed in two ways: by moving the two paths to either the right or to the left of center. When we formed the zeroth-order central fringe by moving the two beams that were exiting the interferometer to the right of center, it was easy to get an in-focus interference pattern and the observed fringe shifts induced by changing the velocity were small and asymmetrical. For this reason, we aligned the interferometer by moving the two beams to the right of center. The asymmetry between the right-side alignment and the left-side alignment may have been caused by uncompensated refraction that took place at the 3.3 mm thick windows. Preliminary data showed that windows that were thinner than 0.1 mm made alignment of the interferometer easy while windows 0.1 mm thick or greater ensured that the windows did not deform when the water velocity changed, but they made alignment more difficult.

Method of observation. Patterns with 7-9 interference fringes were captured with a 9 MP digital camera (AmScope, Irvine, CA) using the Toup View (Ver. x86, 3.7.939) image processing program. We made sure that the fringes in each of the interference patterns in a slow-fast pair would be captured by the camera sensor and recognized by the analysis program. We recorded the voltage produced by the flow meter as we captured gray scale images of the interference fringes. In order to capture images with maximal dynamic range and without saturation, we manually set the exposure time (≈ 10-30 ms) and brightness (-20 to -40) using the line profile command. The gain, contrast and gamma were all kept at 1. The spatial resolution of the collected images was 872 x 654 pixels. We used the maximum frame rate in the software to capture the images. The speed in which we could collect the images was limited by the computer (Dell Pentium 3 GHz, Legacy video board, running Windows XP). We saved the images as .tif files using the gray scale mode in the Image menu.

Method of analysis. We wrote a program called “fizeau” in MATLAB (Appendix) to detect the fringes and to quantify their velocity-difference-dependent shift. The user crops a horizontal strip approximately 40-80 pixels high across the middle of the interference pattern obtained during the faster flow. Experiments where the same image was cropped multiple times show that the error introduced by the cropping technique is less than 0.5 % when using a taller cropping box and as much as 1% when using a shorter cropping box. The program automatically crops the interference pattern generated by the slower flow.

The program then produces intensity profiles for the interference patterns generated by the faster and slower flow (Fig. 6). The intensity profile is not a sine wave, but a frequency-modulated sine wave. Indeed, a close look at any interference pattern shown in any textbook shows that the
patterns are best described by frequency-modulated sine waves. For this reason, we had to determine the fringe shifts individually for each fringe.

The analysis program then finds the peaks and troughs of the intensity profiles in order to identify each fringe (Fig. 7).

Fig. 6: Cropped strips of interference patterns generated by a slower and faster flow rate and average pixel intensity profiles of the cropped images. The velocity difference between the slower and faster flows was 2.029 m/s.

Fig. 7: Fringes identified in the interference patterns generated by the faster and slower flow rates. The velocity difference was 2.029 m/s.
The analysis program determines the fringe shift in the interference patterns caused by the velocity difference between a slower and faster flow rate in each trial by plotting the intensity profile of each fringe generated by the faster flow against the intensity profile of each fringe generated by the slower flow, thus producing an ellipse known as a Bowditch curve [16] or a Lissajous figure. The analysis program fit an ellipse to the data (Fig. 8).

Fig.8: Lissajous figures for each fringe in an interference pattern comparing the average pixel intensity of the fringe produced by the slower velocity (slow intensity) with the average intensity of the same fringe produced by the faster velocity (fast intensity). The experimental data are presented in blue and the fitted ellipses are presented in red. The fringes from left to right are numbered from 1 to 9. The velocity difference was 2.029 m/s and the central fringe (5) shift was 0.078.

Lissajous figures provided a powerful method for comparing the displacement, phase shift or fringe shift between the central zeroth-order fringes under two velocity regimes. The fringe shift was determined with the following formula:

\[ FS = \frac{b}{4a} \]  

(4)

Where, \(FS\) is the fringe shift, \(a\) is the semi-major axis of the fitted ellipse, \(b\) is the semi-minor axis of the fitted ellipse and 4 is the correction factor necessary because the semi-minor axis represents two fringe shifts—one on each side of the peak, and the semi-major axis represents one-half of a wavelength. The zeroth-order central fringe was used for the analysis since it is the most stable fringe and least subject to random fluctuations. Our analysis method is more accurate than any method based on measuring the fringe shift relative to a single line since we take into consideration the movement of the whole zeroth-order central fringe and not just a single vertical line.
Statistical analysis to compare the slope of the regression equation for the experimental values with the slope of the theoretical equation for the Newtonian theory, the Doppler theory, and the Special Theory of Relativity was performed with JMP statistical software (version 10.0.2; SAS Institute Inc.).

**Theoretical analysis.** The predicted fringe shifts are given by the following theoretical formulae [10]:

**Newtonian Theory**  
\[ FS = 1.16 \cdot \frac{2Lm^2}{\lambda c} \]  
(5)

**Special Relativity**  
\[ FS = 1.16 \cdot \frac{2Lm^2}{\lambda c} \left(1 - \frac{1}{n^2}\right) \]  
(6)

**Doppler Theory**  
\[ FS = 1.16 \cdot \frac{2Lu}{\lambda c} \]  
(7)

Where, \( L \) is the total length of the tubes (3.048 m), \( \nu \) is the velocity difference between the fast flow and slow flow in a given trial, \( \lambda \) is the wavelength of the laser \((532 \times 10^9 \text{ m})\), \( c \) is the vacuum speed of light \((2.99 \times 10^8 \text{ m/s})\) and \( n \) is the refractive index of the flowing fluid. The estimated ratio of the maximal velocity where the light beams propagate to the average velocity that is measured is 1.16. The magnitude of the fringe shift with velocity difference is instrument dependent and depends on the wavelength of light, and the length of the tubes, which represents the amount of interaction between the light and the water.

Fizeau [2-4], Michelson & Morley [5], Zeeman [6,7] and Lahaye et al. [9] have already shown that Newtonian theory cannot explain the results of the Fizeau experiment. What is at stake here is whether the fringe shift resulting from the relative motion of the water and the optical system is best described by Eqn. (6), where time is transformed between inertial frames traveling at velocity \( \nu \) relative to each, or by Eqn. (7), where wavelength is transformed between inertial frames traveling at velocity \( \nu \) relative to each.

### 3. Results and Discussion

In the interferometer setup used, the fringes shift to the left when the water velocity changes from fast to slow (Fig. 9).
Systematic error would result in the theoretical lines being less turbulent than at the higher velocities. This could be improved by using an optical table. Systematic error most likely is introduced into the theories or in the experiment. This may be due to the inadequacies in the theories or in the experiment.

Doppler theory is orders of magnitude better than either the Newtonian theory or Special Relativity. This may be due to the differences in the theories or in the experiment. Systematic error may also be introduced by using a more stable water supply. Interestingly enough, while the Doppler-induced fringe shift is the dependent variable in this experiment and the velocity-difference is the independent variable, the Doppler effect is the best method known to measure the velocities of fluids, which is the independent variable here. Even the general public is familiar with the use of ultrasonic Doppler echocardiography to measure the speed and direction of blood flow through blood vessels and the heart and the use of Doppler Magnetic Resonance Imaging to measure blood flow through the brain. The velocities of flowing fluids are also measured with laser Doppler velocimetry (LDV) and laser Doppler anemometry (LDA). Indeed, the optical Doppler effect could be used in an interferometer setup like the one described here to accurately map the structure of the velocity gradient in fluids flowing through pipes. Such an investigation would allow for a better value of the ratio of the maximum velocity to the average measured velocity.

**Fig. 10**: A graph of the fringe shift versus the measured velocity difference. The experimental data are shown as filled circles and the dashed line is the regression line for the experimental data. The blue solid line is the theoretical prediction for the Special Theory of Relativity \((FS = \frac{2\Delta v_{\text{m}}^2}{c^2} \left(1 - \frac{1}{n^2}\right) = 0.0151 \text{ per m/s}\)\), the green solid line is the theoretical prediction for the Doppler theory \((FS = \frac{2\Delta v_{\text{m}}}{c} = 0.0441 \text{ per m/s})\), and the red solid line is the theoretical prediction for the Newtonian theory \((FS = \frac{2\Delta v_{\text{m}}^2}{c^2} = 0.0784 \text{ per m/s})\).

Random error present in the data could be reduced by using a more stable water supply.

The velocities of flowing fluids are measured with laser Doppler velocimetry (LDV) and laser Doppler anemometry (LDA). Indeed, the optical Doppler effect could be used in an interferometer setup like the one described here to accurately map the structure of the velocity gradient in fluids flowing through pipes. Such an investigation would allow for a better value of the ratio of the maximum velocity to the average measured velocity.
Table 1: Statistical F-Tests of Slope of Experimental Data (n = 161) versus Theoretical Slopes.

<table>
<thead>
<tr>
<th>Theory</th>
<th>Predicted Slope</th>
<th>Experimental Slope (x ± SE)</th>
<th>F value</th>
<th>p value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Newtonian</td>
<td>0.0784</td>
<td>0.0419±0.0006</td>
<td>4303.1</td>
<td>&lt; 9.1 × 10^{-117}</td>
</tr>
<tr>
<td>Doppler</td>
<td>0.0441</td>
<td>0.0419±0.0006</td>
<td>15.6</td>
<td>&lt; 1.1 × 10^{-4}</td>
</tr>
<tr>
<td>Special Relativity</td>
<td>0.0151</td>
<td>0.0419±0.0006</td>
<td>2320.5</td>
<td>&lt; 3.8 × 10^{-97}</td>
</tr>
</tbody>
</table>

Note: We ran 161 trials in a week for this experiment in honor of Cornell University [17], where there are 161 stairs to the top of McGraw Tower where the Cornell Chimes reside.

4. Conclusion

It is the motto of scientists in general that “theory guides, experiment decides” [18]. Einstein rejected Newtonian theory because it could not explain the results obtained from experimenting on the optics and electrodynamics of moving bodies [19]. He removed the inadequacy of Newtonian kinematic theory by proposing that time was relative. In explaining the Fizeau experiment, Einstein [1] did not consider the possibility that the Doppler effect may be fundamentally expanded to second order and that the wavelength of electromagnetic waves may also be fundamentally relative. The experiment presented here tested whether the results of a modern repetition of the Fizeau experiment are better explained by the relativity of time as described by the Special Theory of Relativity or by the relativity of wavelength as described by the relativistic Doppler effect.

In discussing the theory-experiment relation, Jan Frercks [20] has described the almost ideal case of an experimental test of theory, “An observable effect is mathematically derived from a fundamental theory, an apparatus capable of detecting this effect is conceived and built, measurements are taken, the data happen to be in full correspondence with the expectation, which corroborates the underlying theory.” In the example presented here, it took us two and a half years of tinkering, and trial and error as we worked to combine the optics, the hydraulics, and the analysis in order to build an interferometer to test whether or not the relativistic Doppler effect could describe and explain the results of the Fizeau experiment when using an interferometer that has the modern advantages of a laser and digital image capture and analysis. We did this, not with “the considerable means, which American scientists have at their disposal” as Zeeman [6] described Michelson & Morley’s repetition of this experiment, but frugally with money from our own pockets. Mirabile dictu, the results of the Fizeau experiment reported here, like the combined results obtained by Fizeau, Michelson & Morley and Zeeman [10], are accounted for better by the relativistic Doppler theory than by either Newtonian theory or the Special Theory of Relativity.

References

Appendix: MATLAB program for analyzing the data

Program: fizeau

% Analysis of fringe displacement in a Fizeau interferometer

% Set Shift Direction
% If the observed fringe shift is from the right to the left when the
% velocity of the water is decreased, set the following variable to 1,
% otherwise if the observed fringe shift is from the left to the right when
% the velocity of the water is decreased, set the following variable to 0.
left=1;

% Set Number of Imgs
% Set 'start' number to at least 101 and set 'numimg' to 101 plus the
% number of trials to be analyzed.
start=101;
numimg=110;

% Initialize the Output Matrix
output = ('Fringe #';1;2;3;4;5;6;7;8;9;10;11;12;13;14;15;16;17;18;19;20);

output{24,1}='Voltage-Velocity Factor'; output{24,2}=0.7714624195;
output{25,1}='Fast Velocity';
output{26,1}='Slow Velocity';
output{27,1}='Change in Velocity';
output{29,1}='Water Factor'; output{29,2}=1.16;
output{30,1}='Special Relativity'; output{30,2}=0.013;
output{31,1}='Doppler Effect'; output{31,2}=0.038;

% Read in the Imgs
for i=start:numimg
    eval(['s' num2str(i) '=imread(''slow'' num2str(i) '.TIF'');']);
    eval(['f' num2str(i) '=imread(''fast'' num2str(i) '.TIF'');']);
end
% Analyze the Images
for j=start:numimg
    eval(['output{1,j-99}=' '''Trial ' num2str(j-100) ''' ';' ]);
    eval(['[output] = imageanalysis(s' num2str(j) ', f' num2str(j) ', j, output, left);'' ']);
end

% Export the output matrix to excel
xlswrite('output.xlsx', output);

Function: imageanalysis

function [output] = imageanalysis(s1, f1, j, output, left)
% Creates output figures using manual cropping

close all

% Crop the images
[s2, rect]=imcrop(s1);
close all
f2=imcrop(f1, rect);

% Calculate means
smean=mean(s2);
fmean=mean(f2);

% Smooth means
smean=smooth(smean, 5);
fmean=smooth(fmean, 5);

% Find troughs using peakfinder
sindex = peakfinder(smean, 50, 175, -1);
findex = peakfinder(fmean, 50, 175, -1);

% Segment the cropped images into individual fringes
slen = length(sindex);
flen = length(findex);
numfringes = slen-1;

if slen == flen
    for i=1:numfringes
        if left == 1
            width = sindex(i+1)-findex(i);
            fringei = [findex(i) rect(2) width rect(4)];
        else
            width = findex(i+1)-sindex(i);
            fringei = [sindex(i) rect(2) width rect(4)];
        end
        eval(['s' num2str(i+2) ' =imcrop(s1, fringei);']);
eval(['f' num2str(i+2) ' =imcrop(f1, fringei);']);
        % Calculate means
        eval(['smean' num2str(i+2) ' =mean(s' num2str(i+2) ');']);
    end
end
eval(['fmean' num2str(i+2) ' = mean(f' num2str(i+2) ');']);

% Smooth means
eval(['smean' num2str(i+2) ' = smooth(smean' num2str(i+2) ', 5);']);
eval(['fmean' num2str(i+2) ' = smooth(fmean' num2str(i+2) ', 5);']);
end
else
    error('slength = %g flength = %g', slength, flength);
end

% Plot Slow and Fast Means
subplot(3,1,3), plot(smean);
axis([0 872 0 255]);
set(gca,'XTick',0:109:872);
set(gca,'YTick',0:51:255);
xlabel('Pixel');
ylabel('Intensity');
str=sprintf('Slow = Blue    Fast = Green');
title(str);
hold all
subplot(3,1,3), plot(fmean);

% Plot Cropped Images
subplot(3,1,1), subimage(s2);
set(gca,'XTick',0:109:872);
set(gca,'YTick',[]);
title('Slow');
xlabel('Pixel');
subplot(3,1,2), subimage(f2);
set(gca,'XTick',0:109:872);
set(gca,'YTick',[]);
title('Fast');
xlabel('Pixel');
eval(['save2word(''output' num2str(j) '.doc')']);

% Plot Segmented Fringes
figure
for i=1:numfringes
    eval(['subplot(2,numfringes,i), subimage(s' num2str(i+2) ');']);
    set(gca,'XTick',[]);
    set(gca,'YTick',[]);
    eval(['subplot(2,numfringes,i+numfringes), subimage(f' num2str(i+2) ');']);
    set(gca,'XTick',[]);
    set(gca,'YTick',[]);
end

% Title the Segmented Fringes
annotation('textbox', [0 0.9 1 0.06], 'string', 'Slow Fringes', 'HorizontalAlignment', 'center');
annotation('textbox', [0 0.45 1 0.06], 'string', 'Fast Fringes', 'HorizontalAlignment', 'center');
eval(['save2word(''output' num2str(j) '.doc')']);
close all

% Plot the Lissajous Figures
for i=1:numfringes

    % Fit an ellipse
    eval(['[semimajor_axis' num2str(i+2) ', semiminor_axis' num2str(i+2) ', x0' num2str(i+2) ', y0' num2str(i+2) ', phi' num2str(i+2) '] = ellipse_fit(smean' num2str(i+2) ', fmean' num2str(i+2) ');']);

    % Calculate fringe shift
    eval(['fs' num2str(i+2) ' = (semiminor_axis' num2str(i+2) '/ semimajor_axis' num2str(i+2) ')/4;']);

    % Plot Lissajous figure
    figure
    eval(['plot(smean' num2str(i+2) ', fmean' num2str(i+2) ');']);
    axis([0 255 0 255]);
    set(gca, 'XTick',0:51:255);
    set(gca, 'YTick',0:51:255);
    xlabel('Slow Intensity');
    ylabel('Fast Intensity');
    str=sprintf('Fringe %i     Experimental Data = Blue     Fitted Ellipse = Red', i);
    title(str);
    hold all

    % Plot fitted ellipse
    color = 'r';
    eval(['ellipse(semimajor_axis' num2str(i+2) ', semiminor_axis' num2str(i+2) ', phi' num2str(i+2) ', x0' num2str(i+2) ', y0' num2str(i+2) ', color);']);
    eval(['save2word(''output' num2str(j) '.doc'')']);
end

% Add calculated shifts to output matrix
for i=1:numfringes
    eval(['output{i+1,j-99}=fs' num2str(i+2) ';']);
end
end

The following functions used in the above analysis programs were written by others and downloaded from www.mathworks.com.

Function: Peakfinder

http://www.mathworks.com/matlabcentral/fileexchange/25500-peakfinder/content/peakfinder.m

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Function: Ellipse

http://www.mathworks.com/matlabcentral/fileexchange/289-ellipse-m/content/ellipse.m

Written by D.G. Long, Brigham Young University, based on the CIRCLES.m original written by Peter Blattner, Institute of Microtechnology, University of Neuchatel, Switzerland, blattner@imt.unine.ch

Function: Ellipse_fit

http://www.mathworks.com/matlabcentral/fileexchange/22423-ellipse-fit/content/ellipse_fit.m

Programmed by: Tal Hendel thendel@tx.technion.ac.il Faculty of Biomedical Engineering, Technion- Israel Institute of Technology, Dec-2008

Function: Save2Word

http://www.mathworks.com/matlabcentral/fileexchange/3149-save2word/content/save2word.m

Suresh E Joel, Mar 6, 2003, Virginia Commonwealth University, Modification of 'saveppt' in Mathworks File Exchange and valuable suggestions by Mark W. Brown, mwbrown@ieee.org.

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